

Lecture 03:
Randomized controlled trials I

PPHA 34600
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From last time: selection is an issue

Recall that there are lots of things we want to estimate.

We need to get around selection bias to do this.

In other words, we need:

$$E[Y_i(1)] = E[Y_i(1)|D_i = 1] = E[Y_i(1)|D_i = 0]$$

and

$$E[Y_i(0)] = E[Y_i(0)|D_i = 0] = E[Y_i(0)|D_i = 1]$$

Regression equivalent:

$$E[\varepsilon_i|D_i] = 0$$

Random assignment as a solution

When treatment status is randomly assigned,

$$F(X, \varepsilon | D = 1) = F(X, \varepsilon | D = 0) = F(X, \varepsilon)$$

In words:

The distribution of **both** observables (X s) **and** unobservables (ε s) is the same for treated and untreated units!

There is **no selection problem** by construction!

Again, but mathier

When D , treatment, is **randomly assigned**:

- D is independent of $Y(0)$ and $Y(1)$
- The distribution of $Y_i(0)|D_i$ is equal to the unconditional distribution
- The distribution of $Y_i(1)|D_i$ is equal to the unconditional distribution
- $E[Y_i(1)|D_i = 1] = E[Y_i(1)]$
- $E[Y_i(0)|D_i = 0] = E[Y_i(0)]$

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As a result:

$$\begin{aligned}\tau^{ATE} &= E[Y_i(1)] - E[Y_i(0)] \\ &= E[Y_i(1)|D_i = 1] - E[Y_i(0)|D_i = 0] \\ &= E[Y_i|D_i = 1] - E[Y_i|D_i = 0]\end{aligned}$$

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We can easily estimate this from data:

$$\hat{\tau}^{ATE} = \overline{Y(1)} - \overline{Y(0)}$$

We can estimate the ATE simply from the difference in means between treated and “control” group.

This bears repeating

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Obvious (?) caveat: We still can't get τ_i , because we only observe i once.

Evaluating an RCT

This is not a class on how to do RCTs

- As always, the devil is in the details
- Field experiments are *hard!*
- But supposing you've got one...

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Basic RCT checklist

- Verify random assignment
- Check compliance with treatment
- Estimate the ATE (or other things...)

What is this experiment trying to learn?

When running an RCT, you want to have a “research question” in mind:

What is the causal effect of [program x] on [outcome y]?

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When running an RCT, you want to have a “research question” in mind:

What is the causal effect of [program x] on [outcome y]?

Why do we need an RCT to study this?

- Program X targets certain individuals
- Individuals who choose to participate look different than non-participants
- Others?

Understanding RCTs

Basic ingredients for an RCT:

- What is the research design?
 - What is the unit of randomization?
 - How was randomization performed?
- What are the outcomes of interest?

Verifying random assignment

Did randomization “work”?

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Testing whether randomization was effective:

- We want T and C to be similar on observables **and** unobservables
- We can only test this for observables
- To check this, we “test for balance”:
- Compare mean outcomes for T vs. C *at baseline* (before treatment) or in fixed characteristics

→ Implementation: Regress $Y_i^{baseline} = \alpha + \tau D_i + \nu_i$

Checking for balance

Three things to check for:

- 1 Did they test for all outcome variables?
- 2 Are differences statistically significant?
- 3 Are magnitudes economically meaningful?

Did assignment to treatment affect treatment status?

Trying to verify whether...

- Units assigned to treatment were actually treated
- Units assigned to control were *not* treated

There is often substantial non-compliance. We'll talk more about exactly how to deal with this issue next time.

Thinking about non-compliance

We will treat this more formally next time

For now, non-compliance changes the interpretation of our estimates:

Rather than asking "What does treatment do to our outcome activities?" ...

... we're asking "What does offering treatment do to our outcome?"

This may be the policy-relevant quantity

We want to estimate the ATE

Recall that the ATE is just:

$$\tau^{ATE} = E[Y_i(1)] - E[Y_i(0)]$$

Since we have random assignment, we can estimate this as:

$$\hat{\tau}^{ATE} = \overline{Y(1)} - \overline{Y(0)}$$

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Regression is a convenient way to do this:

$$Y_i = \alpha + \tau D_i + \varepsilon_i$$

Since our $E[\varepsilon|D_i] = 0$ assumption is satisfied (why?), $\hat{\tau} = \hat{\tau}^{ATE}$

Estimating treatment effects

We'll often see things that look like this:

$$y_{ia} = \alpha + \tau \text{Treat}_{ia} + \gamma \mathbf{X}_a^{\text{baseline}} + \varepsilon_{ia}$$

where:

- y_{ia} are outcomes for household i in area a
- α is a constant
- Treat_{ia} is a treatment dummy (think D_i)
- $\mathbf{X}_a^{\text{baseline}}$ is a set of baseline area controls
- ε_{ia} is an error term

What is this equation estimating?

$$y_{ia} = \alpha + \tau \mathit{Treat}_{ia} + \gamma \mathbf{X}_a^{\text{baseline}} + \varepsilon_{ia}$$

This differs from our basic regression a bit:

- There's an i and an a
- We have $\gamma \mathbf{X}_a^{\text{baseline}}$

Let's unpack each of these in turn...

Randomization by area, data on individuals

We have i -ndividual level data, but a -rea level randomization

Randomizing at a higher level of aggregation is common:

- Some questions can't be answered at i level (no personal bank branches)
- Ethics concerns: can sometimes delay implementation for a whole group; hard for individuals
- Reduce spillovers (more on this later)

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Randomizing at a higher level affects the analysis:

- Interpretation is different (what exactly is treatment?)
- Getting standard errors right requires either:
 - 1 Estimate i -level effects, but cluster at a -level

or

 - 2 Averaging outcomes at the group level (weight by individuals per group)

Adding controls

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Adding bad controls

First rule of RCT club:

- Do **not** control for post-treatment outcomes
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- If treatment affects these outcomes, you can get bias!

Simple example:

- Suppose microfinance impacts business ownership
- By random assignment, households with and without loans have the same potential income
- Once we condition on business ownership, this is no longer true!

We can use simulated data to think about this

Type of household	Potential business ownership		Potential income		Average earnings by ownership	
	Without MF	With MF	Without MF	With MF	Without MF	With MF
Never owner	No	No	1,000	1,500		
Moved by MF	No	Yes	2,000	2,500		
Always owner	Yes	Yes	3,000	3,500		

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- The return to MFI is 500 for everyone...
 - But once we condition on ownership, it looks like the return is 0!
- This is because we don't have random assignment **within** ownership!

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Do not control for post-treatment outcomes!

We can also estimate heterogeneous effects

Heterogeneous effects are straightforward:

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We typically estimate these in two ways:

- 1 Add an **interaction term** to the regression:

$$y_i = \alpha + \tau \text{Treat}_i + \gamma \text{Treat}_i \cdot X_i + \delta X_i + \varepsilon_i$$

→ Make sure to add both the interaction and the base term

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→ Make sure to add both the interaction and the base term

- 2 Estimate the regression **separately** by heterogeneity

→ Equivalent to a *fully* interacted model

Estimate heterogeneity by pre-determined characteristics only!

A note on assumptions for the RCT

We still need several assumptions for the RCT to work:

- $E[Y_i(1)|D_i = 1] = E[Y_i(1)|D_i = 0]$

and

$$E[Y_i(0)|D_i = 1] = E[Y_i(0)|D_i = 0]$$

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- Perfect compliance

→ Kinda. More on this next class

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 $E[Y_i(0)|D_i = 1] = E[Y_i(0)|D_i = 0]$
 - We “get this” via randomization, but only in expectation
- Perfect compliance
 - Kinda. More on this next class
- No spillovers: “SUTVA”
 - Stable Unit Treatment Value Assumption: D_i doesn't affect j 's potential outcomes
 - Kinda. More on this in two classes

Application: Tuition-free college in Michigan

Dynarski, Libassi, Michelmore, and Owen (2020 NBER WP)

Policy challenge:

- Gaps in educational attainment between low- and high-income kids
- These persist among high-achieving kids
- College has big labor market impacts

Intervention:

- Promise of free tuition and fees to UMichigan-Ann Arbor
- Information sent to students (“HAIL” scholarship)

Tuition-free college in Michigan: The experiment

→ **Lesson for you as MPPs:** RCTs are doable in high-stakes contexts!

This is a **group-level randomization design**:

- Population: high-achieving, low-income seniors in public school
- Randomization done at the *school* level (why?)
- Schools stratified by HAIL-eligible populations

Outcomes of interest

Outcome data is administrative information (!)

Outcomes:

- Application to UMich
- Admission to UMich
- Enrollment at UMich
- Other college choices

Other characteristics:

- Student demographics
- Student performance, incl GPA and test scores

Balance?

Characteristic	Mean		P-value
	Control schools	Treated schools	
<i>Region, urbanicity, and distance</i>			
Upper Peninsula	0.150 (0.016)	0.130 (0.015)	0.344
West Central	0.449 (0.022)	0.476 (0.022)	0.359
Southeast	0.401 (0.021)	0.394 (0.022)	0.788
Suburban	0.340 (0.021)	0.360 (0.021)	0.537
City	0.129 (0.015)	0.100 (0.013)	0.148
Rural	0.530 (0.022)	0.540 (0.022)	0.718
Distance from UM	93.2 (3.545)	96.4 (3.673)	0.529

Balance?

Student academic characteristics

Average SAT (or equivalent)	1254 (2.690)	1260 (2.896)	0.194
Average GPA	3.823 (0.006)	3.833 (0.006)	0.208
Proportion limited English proficient	0.002 (0.001)	0.004 (0.001)	0.410
Proportion receiving special education services	0.009 (0.003)	0.013 (0.004)	0.367
Proportion who sent ACT/SAT scores to UM	0.365 (0.015)	0.377 (0.016)	0.695
UM application rate in 2015	0.067 (0.004)	0.055 (0.004)	0.016
Missing 2015 UM application rate	0.004 (0.003)	0.020 (0.006)	0.015

Balance?

Characteristic	Mean		P-value
	Control schools	Treated schools	
<i>School size</i>			
# of 11th grade students in school	189.1 (0.003)	175.1 (0.006)	0.055
# of HAIL students in school	3.8 (0.140)	3.9 (0.163)	0.649
F-test for joint significance: p-value			0.0004
Number of schools	526	500	1,026
Number of students	1,978	1,932	3,910

Compliance?

Since we observe the outcomes for all students, and therefore all schools, there is no attrition due to non-response. We do not observe whether a student actually receives the information packet (i.e. is effectively treated), and students assigned to the control group cannot be treated, so we do not adjust for non-compliance.

Regression specification and parameters of interest

These authors very simply estimate (modified for our notation):

$$Y_j = \alpha + \tau D_j + \gamma S_j + \beta \mathbf{X}_j + \varepsilon_j$$

where:

- Y_j is our outcome for school j
- D_j is our treatment indicator
- S_j is a stratum fixed effect
- \mathbf{X}_j are controls
- ε_j is an error term

Note: Data are collected at the individual level, but collapsed to the school-(cohort) level

Findings

Outcome	Treatment effect		Control mean
Applied	0.416 (0.021)	0.413 (0.019)	0.259
Admitted	0.174 (0.019)	0.163 (0.017)	0.149
Enrolled	0.149 (0.018)	0.141 (0.016)	0.117
Strata dummies	X	X	
Covariates		X	
Number of schools	1,026		
Number of students	3,910		

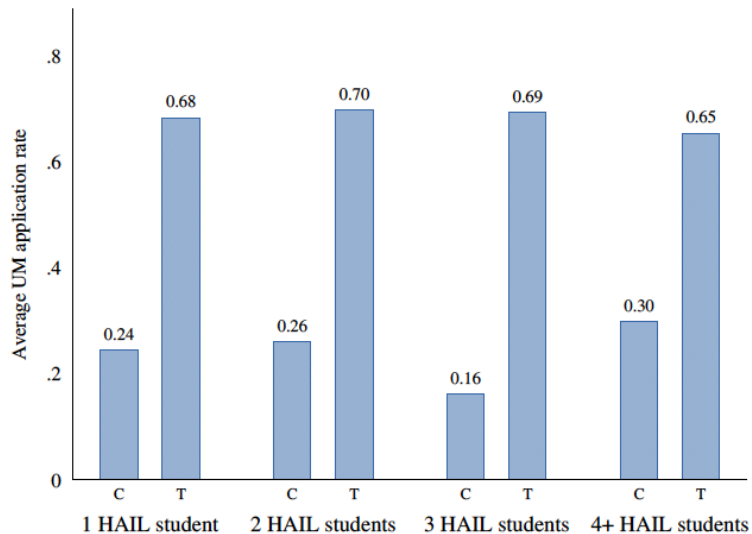
Findings

College attended	Treatment effect	Control mean
Highly competitive or above	0.146 (0.018)	0.135
UM	0.146 (0.016)	0.107
Highly competitive or above other than UM	0.000 (0.007)	0.028
Four-year	0.074 (0.020)	0.675
Two-year	-0.035 (0.013)	0.116
Any	0.039 (0.018)	0.791
In Michigan	0.045 (0.020)	0.727
Public in Michigan	0.062 (0.021)	0.645
Outside Michigan	-0.006 (0.010)	0.064
Number of schools		1,026
Number of students		3,910

Findings

College attended	Attended fall following high school graduation		Attended two consecutive falls following high school graduation	
	Treatment effect	Control mean	Treatment effect	Control mean
Highly competitive or above	0.153 (0.024)	0.129	0.135 (0.023)	0.126
UM	0.147 (0.022)	0.104	0.128 (0.022)	0.102
Four-year	0.091 (0.028)	0.651	0.109 (0.029)	0.557
Any	0.057 (0.025)	0.779	0.079 (0.027)	0.683
Number of schools		529		
Number of students		2,108		

Heterogeneity



TL;DR:

- ① RCTs are great!
- ② Experiments solve our selection problem
- ③ Be very careful with adding controls